

$$[2][a] \left| \lim_{x \rightarrow -1^+} \frac{\frac{2}{x+3} - 1}{\frac{3}{2x-1} + 1} \right| = \lim_{x \rightarrow -1^+} \frac{\frac{2}{x+3} - 1}{\frac{3}{2x-1} + 1} \cdot \frac{(x+3)(2x-1)}{(x+3)(2x-1)}$$

$\frac{1}{2}$

$\frac{0}{0}$

THIS MUST BE CORRECT

$$= \lim_{x \rightarrow -1^+} \frac{2(2x-1) - (x+3)(2x-1)}{3(x+3) + (x+3)(2x-1)} \quad \frac{1}{2}$$

$$= \lim_{x \rightarrow -1^+} \frac{4x - 2 - (2x^2 + 5x - 3)}{3x + 9 + (2x^2 + 5x - 3)}$$

$$= \lim_{x \rightarrow -1^+} \frac{-2x^2 - x + 1}{2x^2 + 8x + 6} \quad \frac{1}{2}$$

$$= \lim_{x \rightarrow -1^+} \frac{(x+1)(-2x+1)}{(x+1)(2x+6)}$$

$$= \lim_{x \rightarrow -1^+} \frac{-2x+1}{2x+6} = \frac{-2(-1)+1}{2(-1)+6} = \frac{3}{4} \quad \star$$

GRADE AGAINST ONLY 1 VERSION

OR

$$\left| \lim_{x \rightarrow -1^+} \frac{\frac{2}{x+3} - 1}{\frac{3}{2x-1} + 1} \right| = \lim_{x \rightarrow -1^+} \frac{\frac{2-(x+3)}{x+3}}{\frac{3+(2x-1)}{2x-1}}$$

$\frac{1}{2}$

THIS MUST BE CORRECT

$$= \lim_{x \rightarrow -1^+} \frac{\frac{-x-1}{x+3}}{\frac{2x+2}{2x-1}} \quad 1$$

$$= \lim_{x \rightarrow -1^+} \frac{-(x+1)}{x+3} \cdot \frac{2x-1}{2(x+1)}$$

$$= \lim_{x \rightarrow -1^+} \frac{1-2x}{2(x+3)} = \frac{1-2(-1)}{2(-1+3)} = \frac{3}{4}$$

$\frac{1}{2}$

$\star$

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(1/2)

$$\lim_{x \rightarrow -1^-} \frac{x + \sqrt{x+2}}{1-x^2} = \lim_{x \rightarrow -1^-} \frac{x + \sqrt{x+2}}{1-x^2} \cdot \frac{x - \sqrt{x+2}}{x - \sqrt{x+2}}$$

0/0

THIS MUST
BE CORRECT

$$= \lim_{x \rightarrow -1^-} \frac{x^2 - (x+2)}{(1-x^2)(x - \sqrt{x+2})}$$

$$= \lim_{x \rightarrow -1^-} \frac{x^2 - x - 2}{(1-x^2)(x - \sqrt{x+2})} \quad (1/2)$$

$$= \lim_{x \rightarrow -1^-} \frac{(x-2)(x+1)}{(1-x)(1+x)(x - \sqrt{x+2})}$$

$$= \lim_{x \rightarrow -1^-} \frac{x-2}{(1-x)(x - \sqrt{x+2})} \quad (1/2)$$

$$= \frac{-1-2}{(1-1)(-1-\sqrt{1+2})} = \frac{-3}{2(-2)} = \frac{3}{4} \quad (\star)$$

$$\lim_{x \rightarrow -1} f(x) = \frac{3}{4} \quad (1/2)$$

BOTH 1-SIDED LIMITS
MUST EQUAL $\frac{3}{4}$
FOR (1/2) POINT TOTAL

[b] NO, SINCE $f(-1)$ DNE (1/2)

[3] $\left(\frac{1}{2} \right) \quad -1 \leq \cos \frac{1}{\sqrt[3]{x}} \leq 1 \quad \text{FOR ALL } x \in (-\infty, \infty)$

$\left(\frac{1}{2} \right) \quad -x^6 \leq x^6 \cos \frac{1}{\sqrt[3]{x}} \leq x^6 \quad \text{SINCE } x^6 \geq 0$

$\lim_{x \rightarrow 0} -x^6 = -0^6 = 0 = \lim_{x \rightarrow 0} x^6 \quad (1)$

BY SQUEEZE THEOREM, $\lim_{x \rightarrow 0} x^6 \cos \frac{1}{\sqrt[3]{x}} = 0 \quad \left(\frac{1}{2} \right)$

$\left(\frac{1}{2} \right)$

$$[4] \lim_{x \rightarrow -1^+} [1 + f(x)]^2 = \lim_{x \rightarrow -1^+} (1 + f(x)) \cdot \lim_{x \rightarrow -1^+} (1 + f(x))$$

THIS MUST BE CORRECT

$$= \left[\lim_{x \rightarrow -1^+} (1 + f(x)) \right]^2 \quad \left(\frac{1}{2} \right)$$

$$= \left[\lim_{x \rightarrow -1^+} 1 + \lim_{x \rightarrow -1^+} f(x) \right]^2 \quad \left(\frac{1}{2} \right)$$

$$\left(\frac{1}{2} \right) [1 + 0]^2 = 1$$

THESE MUST BE CORRECT

$$\lim_{x \rightarrow -1^-} [1 + f(x)]^2 = \left[\lim_{x \rightarrow -1^-} 1 + \lim_{x \rightarrow -1^-} f(x) \right]^2 \quad \left(\frac{1}{2} \right)$$

$$= [1 + -2]^2 = 1$$

$$\lim_{x \rightarrow -1} [1 + f(x)]^2 = 1 \quad \left(\frac{1}{2} \right) \quad \left(\frac{1}{2} \right)$$

[5] $\cos x, 2$ ARE CONT. FOR ALL x $\left(\frac{1}{2}\right)$

$\sqrt{x}$ IS CONT FOR $x > 0$

$2 - \sqrt{x}$ IS CONT FOR $x > 0$

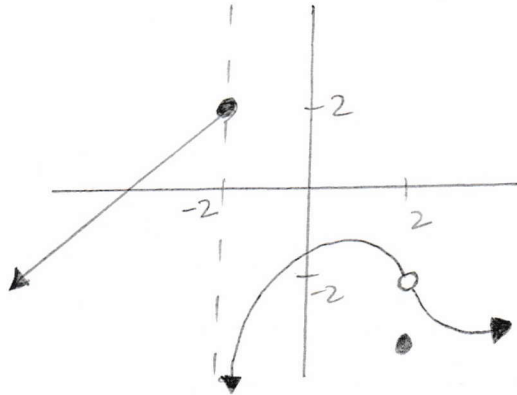
$\left(\frac{1}{2}\right)$ MUST HAVE BOTH

$\frac{\cos x}{2 - \sqrt{x}}$ IS CONT FOR $x > 0$ EXCEPT WHERE $2 - \sqrt{x} = 0$ $\left(\frac{1}{2}\right)$

IE. $2 = \sqrt{x}$

IE. $x = 4$ $\left(\frac{1}{2}\right)$

[6]



GRADED BY ME
(MANY SOLUTIONS
POSSIBLE)

$$[7] \lim_{x \rightarrow 1} \frac{x^2 - 2x + 1}{x^2 - 3x + 2} = \lim_{x \rightarrow 1} \frac{(x-1)^2}{(x-1)(x-2)} = \lim_{x \rightarrow 1} \frac{x-1}{x-2} = \frac{0}{-1} = 0$$

$\frac{0}{0}$ $\frac{1}{2}$ $\frac{1}{2}$

$\frac{1}{2}$ $\cos^{-1} x$ IS CONT. AT $x=0$ SINCE $\cos^{-1} x$ IS CONT. AT ALL $x \in (-1, 1)$

$$\lim_{x \rightarrow 1} \cos^{-1} \frac{x^2 - 2x + 1}{x^2 - 3x + 2} = \lim_{t \rightarrow 0} \cos^{-1} t = \cos^{-1} 0 = \frac{\pi}{2}$$

$t = \frac{x^2 - 2x + 1}{x^2 - 3x + 2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$